

$$\sin^2 x - \sqrt{2}\cos(2x - P/4)=1$$

$$\sin^2 x - \sqrt{2}\cos 2x \cdot \cos(P/4) - \sqrt{2}\sin 2x \cdot \sin(P/4)=1$$

$$\sin^2 x - \cos 2x - \sin 2x=1$$

$$\sin^2 x - 2\cos^2 x + 1 - 2\sin x \cdot \cos x=1$$

$$\sin^2 x - 2\cos^2 x - 2\sin x \cdot \cos x=0$$

$$u = \sin x$$

$$v = \cos x$$

$$u^2 - 2v^2 - 2uv=0$$

Однородное - это когда каждое слагаемое имеет одинаковую степень

$$\deg(u^2)=2$$

$$\deg(uv)=1+1=2$$

$$u^2 - 2v^2 - 2uv=0$$

$$\text{Пусть } v=0 \Rightarrow u^2=0 \Rightarrow u=0$$

$\cos x=0 \Rightarrow \sin x=0$  а такого не может быть  $\Rightarrow$  мы можем делить на  $v^2$

$$u^2 - 2v^2 - 2uv=0 \mid :v^2$$

$$(u/v)^2 - 2 - 2(u/v)=0$$

$$u/v=t$$

$$t^2 - 2t - 2=0$$

$$D=1+2=3$$

$$t_1=(1-\sqrt{3})$$

$$t_2=(1+\sqrt{3})$$

$$u/v=1-\sqrt{3}$$

$$\sin x / \cos x = 1 - \sqrt{3}$$

$$\operatorname{tg} x = 1 - \sqrt{3}$$

$$x = \operatorname{arctg}(1 - \sqrt{3}) + Pn$$

$$\sin x / \cos x = 1 + \sqrt{3}$$

$$\operatorname{tg} x = 1 + \sqrt{3}$$

$$x = \operatorname{arctg}(1 + \sqrt{3}) + Pn$$

Ответ:  $\operatorname{arctg}(1 - \sqrt{3}) + Pn$ ;  $\operatorname{arctg}(1 + \sqrt{3}) + Pn$ .

$$\sin^3 3x - 4\sin^2 3x \cdot \cos 3x + 3\sin 3x \cdot \cos^2 3x = 0 : \sin^3 x \cdot 3$$

$$\sin 3x = u$$

$$\cos 3x = v$$

$$u^3 - 4u^2v + 3u^2v^2 = 0 \mid :v^3$$

Пусть  $v=0 \Rightarrow u=0 \Rightarrow \sin 3x=0$  &&  $\cos 3x=0$  такого быть не может

$$u^3/v^3 - 4u^2/v^2 + 3u/v = 0$$

$$u/v=t$$

$$t^3 - 4t^2 + 3t = 0$$

$$t(t^2 - 4t + 3) = 0$$

$$t_1 = 0$$

$$t^2 - 4t + 3 = 0$$

$$t_2 = 3$$

$$t_3 = 1$$

$$u/v=0$$

$$\sin 3x / \cos 3x = 0$$

$$\sin 3x = 0$$

$$3x = Pn$$

$$x = Pn/3$$

$$u/v=1$$

$$\sin 3x / \cos 3x = 1$$

$$\operatorname{tg} 3x = 1$$

$$3x = P/4 + Pn$$

$$x = P/12 + Pn/3$$

$$u/v=3$$

$$\sin 3x / \cos 3x = 3$$

$$\operatorname{tg} 3x = 3$$

$$3x = \operatorname{arctg}(3) + Pn$$

$$x = \frac{1}{3}(\operatorname{arctg}(3) + Pn)$$

Ответ:  $Pn/3$ ;  $P/12 + Pn/3$ ;  $\frac{1}{3}(\operatorname{arctg}(3) + Pn)$ .

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$$(2\sin x \cdot \cos x - \cos^2 x) / (2\cos x - \sin x) = 0$$

$$\begin{cases} 2\sin x \cdot \cos x - \cos^2 x = 0 \\ 2\cos x - \sin x \neq 0 \end{cases}$$

$$2\sin x \cdot \cos x - \cos^2 x = 0$$

$$\sin x = u$$

$$\cos x = v$$

$$2uv - v^2 = 0 \mid u^2$$

$$2v/u - v^2/u^2 = 0$$

$$v/u=t$$

$$2t - t^2 = 0$$

$$t^2 - 2t = 0$$

$$t_1 = 0$$

$$t_2 = 2$$

$$v/u=0$$

$$\operatorname{ctg} x = 0$$

$$x = P/2 + Pn$$

$$\operatorname{ctg} x = 2$$

$$x = \operatorname{arctg}(2) + Pn$$

Ответ:  $P/2 + Pn$ ;  $\operatorname{arctg}(2) + Pn$ .